## TEACHER EDITION

# PRE-ALGEBRA <br> USING LEGO BRICKS 



Dr. Shirley Disseler

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# Pre-Algebra Using LEGO ${ }^{\circledR}$ Bricks-Teacher Edition 

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- Suggested Brick Inventory
- Student Assessment Chart
- Brick Modeling Chart for Constants and Variables
- Baseplate Paper


## ABSOLUTE VALUE

## Students will learn/discover:

- How positive and negative numbers are used together to describe quantities with opposite directional values (integer value) using real-world examples such as temperature, elevation, and credit/debit
- How to use a number line to identify negative and positive numbers and understand that numbers exist that are less than zero
- How to identify absolute value as the distance of a number from zero


## Why is this important?

Understanding positive and negative numbers is important in many contexts. Being able to identify numbers less than zero (negative numbers) allows for better understanding of many real-world situations, including money, time, speed, location, and temperature. The accounting credit and debit system uses negative and positive numbers to describe losses and gains. Negative and positive numbers describe below and above freezing. Sea level and altitude descriptions also use negative and positive numbers. Sports such as golf and football use positive and negative numbers to note above and below par, or gains and losses of yards. Students should understand the relationship of integers in terms of below or above a given specification. In terms of speed, for example, one could drive above or below the speed limit, which can be noted by +/- signs.


SUGGESTED BRICKS

| SUGGES | ED BRIC |
| :---: | :---: |
| Size | Number |
| 1x1 | 1 blue |
| $1 \times 2$ | $\begin{aligned} & 10 \text { red } \\ & 10 \text { green } \end{aligned}$ |
| $1 \times 3$ | 1 white 3 red 3 green |
| $1 \times 4$ | 1 white 3 red 3 green |
| 1x6 | $\begin{aligned} & 1 \text { red } \\ & 1 \text { green } \end{aligned}$ |
| $1 \times 10$ | $\begin{aligned} & 1 \text { red } \\ & 1 \text { green } \end{aligned}$ |
| $1 \times 16$ | 2 white |

Note: Using a baseplate helps keep the bricks in place. Two baseplates are suggested for these activities. ,

## Vocabulary:

- Integer: A whole number that can be positive, negative, or zero
- Positive number: A whole number greater than zero
- Negative number: A whole number less than zero
- Integer value: The location of any integer on a number line relative to zero which informs whether it carries a negative or positive sign as an identifier


## How to use the companion student book,

 Pre-Algebra Using LEGO ${ }^{\circledR}$ Bricks-Student Edition:- After students build their models, have them draw the models and explain their thinking in the Student Edition. Recording the models on paper after building them with bricks helps reinforce the concepts being taught.
- Discuss the vocabulary for each lesson with students as they work through the Student Edition.
- Use the chapter assessments in the Student Edition to gauge student understanding of the content.


## Part 1: Show Them How

In this chapter, integer value and absolute value will be discussed and modeled. Understanding what an integer is and what absolute value means are key ideas for algebraic thinking about numbers. Throughout this book, red bricks will be used to model negative numbers, and green bricks will be used to model positive numbers.

Have students begin by building a number line using two white 1 x 16 bricks, one white $1 \times 4$ brick, and one white $1 \times 3$ brick across two baseplates. Place one blue 1 x 1 brick on top of the bricks, directly in the center. It should be a long row of bricks: one blue stud on top, with 19 white studs on


Have students place one green 1 x 6 brick above the number line starting at zero and ending at the sixth stud.


Have students place a red $1 \times 6$ brick on the number line on


Explain to students that these two bricks show the same distance from zero. The distance a number is from zero is its absolute value. The absolute value here is 6 , which is written as $|6|$.

In this model, the red brick indicates a negative direction and the green brick represents a positive direction. Discuss the idea that a negative number lies on the number line to the left of zero, while a positive number lies to the right of zero. These numbers are called integers and their value is known as the integer value.

Point out that this model shows +6 and -6 .

Have students remove the two $1 \times 6$ bricks and model the following pairs of integers.

## Problem \#1: Model -4 and +4

Ask students which bricks they will use for the model. (Answer: one red 1x4 brick and one green $1 \times 4$ brick)

Have students build models of -4 and +4 .

Ask students: How do you know the absolute value when you look at your completed model? (Answer: the absolute value is shown by the distance from zero on the number line, which is 4 in both directions)

Have students draw the model and label it. Have students identify the absolute value.


Problem \#2: Model +10 and -10
Ask students which bricks they will use for the model. (Answer: 1 red 1x10 brick and 1 green $1 \times 10$ brick)

Have students build models of +10 and -10 .

Ask students: How do you know the absolute value when you look at your completed model? (Answer: the absolute value is shown by the distance from zero on the number line, which is 10 in both directions)

Have students draw the model and label it. Have students identify the absolute value.


Discuss with students that +10 means you have 10 more than zero, and -10 means you have 10 less than zero (it indicates subtraction). In other words, when you have 10 and then give 10 , you have zero. This means that there is a one-to-one ratio on both sides of the zero on the number line and they cancel each other out. This is called a zero pair. Note: This concept will be important in computation in later chapters in this book.

## Problem \#3: Model -2 and +2

Have students build models of -2 and +2 .
Ask students to define what this model shows, based on their knowledge from previous models. (Answer: 2 is the number's distance from zero; 2 is the absolute value)

## Part 2: Show What You Know

1. Build a model to show -8 and +8 on a number line. Draw your model and label each number.

What is the absolute value of -8? Answer: $|8|$
Explain how you know the absolute value. Answer: 8 is located exactly 8 studs from zero, which is its absolute location. -8 is located exactly 8 spaces to the left of zero and 8 is located exactly 8 spaces to the right of zero.
2. Build a model to show two numbers whose absolute value is 12 . Use red and green bricks to show the positive and negative numbers. Hint: You will need several bricks to model each of these numbers. Draw and label your model.

Which bricks did you use to make the model? Answer: Various possibilities

What two numbers did you model? Answer: -12 and +12
3. Model two numbers that make a zero pair. Draw and label your numbers. Identify the absolute value of your numbers.

What numbers did you model?
Which bricks did you use to model your numbers?
Solutions will vary

